Worksheet 7

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- 1. 5 students are giving a make-up quiz. The probability of any of them scoring more than 25 is 0.6. Let X be the number of students who get over 25.
 - a. Identify the distribution of X and its parameters.
 - b. What is the probability that none of the students score over 25 ?
 - c. What is the probability that at least one of them score over 25 ?
 - d. What is the probability that all of them score over 25 ?

1 - 0.9222 = 0.0778(0.6)'(1-0.6)SCS

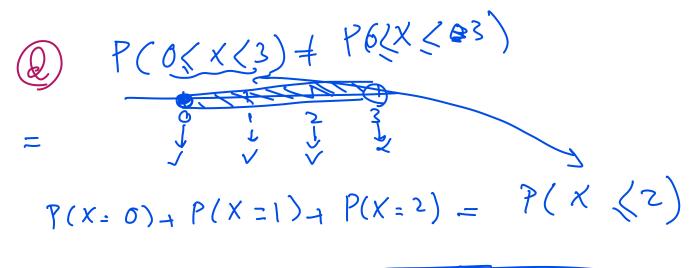
2. A six-sided die is rolled 6 times. Let X denote the number of times an even number showed up.

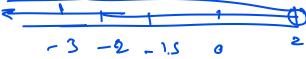
- a. What is the probability of the event happening? That is, the probability of getting an even number. $P(exentrumbed in a \land Pcol() = \frac{1}{2} = \frac{3}{4}$
- b. What distribution will X follow? Identify the parameters.
- c. Calculate P[X = 2].

d. Calculate
$$P[0 \le X < 3]$$

 $P[x = 1]$
 $P[x = 2]$
 $P[x = 2]$

$$0.3438 = 0.1894 = 0.2344$$





= 0.34 38

3. Acme Corporation's helpdesk gets 4 calls per day on average. They think the number of calls follows a Poisson distribution. a. What is the probability that they get 3 calls or less on a given day? b. What is the probability that they get no calls on given day? (7X)=7 E(X) c. What is the probability that they get exactly 3 calls? d. What is the expected number of calls in a week? e. What is the standard deviation for calls in a day? Vor(x) = E(x) = 4P(X < 3) = 0,4335 Sd (x) = Var(x) = 14 = 2 P(X 6 = 0.01883 P(X=0) =PIX: = 3) = ?? P(x (4)31 3 Ø P(X=2) + P(X=1) + P(X=0) P(X=2) + P(X=1) - 1 P(X=0)P(X=3) $P(X \leq 3)$ _P(X <2) $P(X - 3) = P(X \leq 3) - P(X \leq 2)$ 0.4335 - 0.2381 = 0.1954

- 4. The number of flaws in an optic fiber cable follows a Poisson Distribution. The average number of flaws in 50 m is 1.5. Let x = number of flaws in 50 m.
 - a. What is the probability of exactly 2 flaws in 100 m ?
 - b. What is the probability of 3 flaws or less in 150 m ?

- 5. X is a Uniformly distributed random variable that has maximum and minimum values of 10 and 50.
 - a. What is the density function and its graph?
 - b. Calculate the mean of X.
 - c. Calculate P[10 < X < 20] and mark the corresponding area on the graph from (a).
 - d. Calculate P[25 < X < 45] and mark the corresponding area on the graph from (a).
- e. Find P[X = 22.5]. f(x) =_ arxcb 2 6-a) 10 ZXZ 50 f(x) = 0.w 50 10 30 4 s 0 $\frac{a+b}{2} = \frac{10+50}{2}$ E(x) = <u>-</u> 30 $P(10 < X < 25) - R area Veren M = \frac{1}{40} + (20 - 10) = \frac{1}{4}$

(d)
$$P(zs(X \angle 4s)) = Green one plane)= \frac{1}{40}(4s - 2s) = \frac{1}{2} = 0.5$$